

2.0

1)

$$\sigma = \pi (2a)^2$$

$$1.26 \times 10^{-16}$$

$T = 300K$

Dados $\sigma = 3.52 \times 10^{-16} \text{ cm}^2$

$m_N = 2.32 \times 10^{-23} \text{ g}$?

$\lambda = \frac{1}{n\sigma} \rightarrow n = \rho$

m_N

Nitrogeno: $0.1 \text{ nm} = 28 \text{ nucleons}$

$\rho_{\text{ox}} = 1.2 \text{ Kg/m}^3 = 0.0012 \text{ g/cm}^3$

$K_B = 1.38 \times 10^{-23} \text{ J/K}$

$v_{\text{rms}} = \sqrt{\frac{3 K_B T}{m_N}} \rightarrow t = \lambda / v$

$n = \rho = 0.0012 \text{ g/cm}^3 = 5.17 \times 10^{19} \text{ cm}^{-3}$

$28 \times m_H \quad 2.32 \times 10^{-23} \text{ g}$

$\lambda = \frac{1}{n\sigma} = \frac{1}{5.17 \times 10^{19} \text{ cm}^{-3} \cdot 3.52 \times 10^{-16} \text{ cm}^2} = \frac{1}{18057.6 \text{ cm}^{-1}} = 5.54 \times 10^{-5} \text{ cm}$

$v_{\text{rms}} = \sqrt{\frac{3 K_B T}{m_N}} = \sqrt{\frac{3 \cdot 1.38 \times 10^{-23} \text{ J/K} \cdot 300K}{2.32 \times 10^{-26} \text{ Kg}}} = \sqrt{\frac{1.242 \times 10^{-20}}{2.32 \times 10^{-26}}} = 731.7 \text{ m/s}$

$J = n \cdot \lambda \cdot v \cdot K_B \cdot T \quad 515$

73170 cm/s

Então $t = \lambda = \frac{5.54 \times 10^{-5}}{73170} = 7.57 \times 10^{-10} \text{ s}$

6×10^{-10}

2)

$$T_{atm} = ? \quad w \quad T_e = ?$$

$$T_{atm} = \frac{T_e^4 - 3T_e^4}{4} (\epsilon_v + \frac{2}{3}) \rightarrow \text{Para o topo da atmosfera } \epsilon_v = 0$$

\therefore

$$T_e^4 = \frac{8}{4} (5777)^4 (0 + \frac{2}{3}) = (5777)^4 \cdot \frac{4}{3}$$

$$T_e = \sqrt[4]{\frac{8}{4} (5777)^4 (0 + \frac{2}{3})} = 4858 \text{ K} \rightarrow T_{topo}$$

Após a inversão $T_e = 1,18 \Rightarrow$

$$\begin{cases} T_e = 1,18 T \\ T = 0,84 T_e \end{cases}$$

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8) $r_p \approx 10^{-15} \text{ m}$

$e = 1.6 \times 10^{-19}$

3) $v_{rms} = 10 \text{ km/s}$

Para 2 protones colisionando

a) $T_{c \text{ Sol}} = 1.44 \times 10^7 \text{ K}$

↳ ultraproximo a la superficie

$\frac{1}{2} \mu m \bar{v}^2 = \frac{3}{2} kT = \frac{Z_1 Z_2 e^2}{4\pi\epsilon_0 r}$

① $\frac{1}{2} \mu m \bar{v}^2 = \frac{1}{2} \mu m (10 \text{ km/s})^2 = \frac{1}{2} \mu m 100 \cdot \left(\frac{3kT}{m_p} \right)$

↳ $v_{rms} = \sqrt{\frac{3kT}{m_p}}$ u $\mu m = \frac{m_p}{2}$

② $\mu m 100 \frac{3kT}{m_p} = \frac{e^2}{4\pi\epsilon_0 r} \rightarrow T = \frac{e^2}{4\pi\epsilon_0 r} \cdot \frac{m_p}{3k} \cdot 2$

$\frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \text{ N.m}^2$

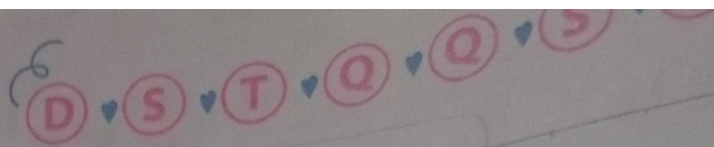
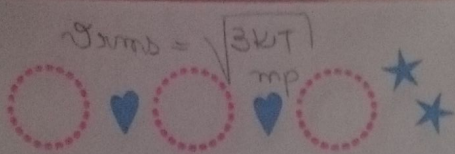
③ Substituyendo los valores

$T = \frac{8.99 \times 10^9 \cdot (1.6 \times 10^{-19})^2 \cdot m_p}{3 \cdot (1.38 \times 10^{-23}) \cdot 100}$
 $= \frac{8.99 \times 10^9 \cdot (1.6 \times 10^{-19})^2 \cdot 4}{10^{-15} \cdot 300 \cdot (1.38 \times 10^{-23})} = \frac{9.2 \times 10^{-23}}{4.14 \times 10^{-36}} = 2.2 \times 10^8 \text{ K}$

Temperatura necesaria

④ Comparando c/ Sol $T_c = 1.44 \times 10^7 \text{ K}$

$\frac{T}{T_{c0}} = 15.2 \rightarrow T = 15.2 T_{c0}$
 $T_{c0} = 0.06 T$



b) $n d v = n \left(\frac{m}{2\pi kT} \right)^{3/2} e^{-mv^2/2kT} 4\pi v^2 dv$

①

Reason $n_{10}/n = ?$

$$\frac{n_{10}}{n} = \frac{e^{(-m(10v_{rms})^2/2kT)}}{e^{(-mv_{rms}^2/2kT)}} \cdot \frac{(10v_{rms})^2}{(v_{rms})^2}$$

$$\frac{n_{10}}{n} = \left[\frac{10v_{rms}}{v_{rms}} \right]^2 \exp \left[\frac{-mp 100 v_{rms}^2 + mp v_{rms}^2}{2kT} \right]$$

$$= 100 \exp \left[\frac{-99 mp v_{rms}^2}{2kT} \right]$$

② Substituting values

$$\frac{n_{10}}{n} = 100 \exp \left[\frac{-99 \cdot \cancel{mp} \cdot 3kT}{2kT \cdot \cancel{2mp}} \right] = 100 e^{-297/2} = 100 e^{-148,5}$$

$$\therefore \frac{n_{10}}{n} = 100 \cdot 3,22 \times 10^{-65} = 3,22 \times 10^{-63} \quad // \quad 5,7 \times 10^{-31}$$



c) $M_0 = 1,989 \times 10^{-30} \text{ kg}$
 $m_H = 1,673 \times 10^{-27} \text{ kg}$

①

Número de nucleons $= \frac{M_0}{m_H} = \frac{1,989 \times 10^{-30}}{1,673 \times 10^{-27}} = 1,19 \times 10^{-3}$ //

②

$n = 1,2 \times 10^{57} \times 5,67 \times 10^{-34} = 6,8 \times 10^{23}$ nucleons
 c/ $v = 10 v_{th}$

$t = E / L_0 = 1,88 \times 10^{-12} \text{ s}$

$\approx 11 \text{ cm/s}$

4) a) $(\Delta \lambda)_{\text{rel}} = \frac{2\lambda}{c} \sqrt{\frac{2kT \ln 2}{m}}$

$v_{\text{turb}} = 0$

Hen: $\lambda = 6563 \text{ \AA} = 656,28 \text{ nm}$ $m = M_0 = 1,989 \times 10^{-30} \text{ kg}$
 $T = T_e = 5777 \text{ K}$ $k = 1,38 \times 10^{-23} \text{ J/K}$
 $c = 3 \times 10^8 \text{ m/s}$

$(\Delta \lambda)_{\text{rel}} = \frac{2 \cdot 6,563 \times 10^{-7}}{3 \times 10^8} \sqrt{\frac{2 \cdot 1,38 \times 10^{-23} \cdot 5777 \cdot \ln 2}{(1,989 \times 10^{-30}) \cdot 1,67 \times 10^{-27}}}$

$= \frac{1,31 \times 10^{-6}}{3 \times 10^8} \sqrt{\frac{1,1 \times 10^{-19}}{1,989 \times 10^{-30}}} = 4,34 \times 10^{-15} \cdot 2,35 \times 10^{-25}$

$\rightarrow (\Delta \lambda)_{\text{rel}} = 1,03 \times 10^{-39} \text{ m} \times 0,03559 \text{ nm}$



b)

→ equamulo
 $v_{turb} : 4 \text{ km/s} = 4000 \text{ m/s}$

$v_{turb} = 400 \text{ m/s}$

$$(\Delta \lambda)_{\lambda} = \frac{2\lambda}{c} \sqrt{\left(\frac{2kT}{m} + v_{turb}^2 \right) \ln 2}$$

$$= 4,37 \times 10^{-15} \cdot \sqrt{\left(\frac{1,1 \times 10^{-19}}{1,989 \times 10^{-30}} \right) + 7000^2 \ln 2}$$

$$= 4,37 \times 10^{-15} \cdot \sqrt{5,53 \times 10^{-50} + 3,4 \times 10^{-7}}$$

$$= 4,37 \times 10^{-15} \cdot 5830,9 = 2,6 \times 10^{-11}$$

c)

$$\frac{(v_{turb})^2}{2kT/m} = \frac{(4000)^2}{2 \cdot 1,38 \times 10^{-23} \cdot 5477} = \frac{1,6 \times 10^{37}}{1,59 \times 10^{-19}} = 6,12 \times 10^{56}$$

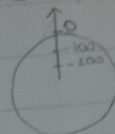
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5) $\rho = 2,2 \times 10^{-4} \text{ Kg m}^{-3}$ | $\lambda_1 \rightarrow K_{\lambda 1} = 0,026 \text{ m}^2 \text{ Kg}^{-1}$
 $T = 5777 \text{ K}$ | $\lambda_2 \rightarrow K_{\lambda 2} = 0,03 \text{ m}^2 \text{ Kg}^{-1}$

$\tau = 2/3$

$\tau_\lambda = 0$ ou p

$dZ_\lambda = -K_{\lambda} \rho dS$



1) $\tau_\lambda = -0,026 \cdot 2,2 \times 10^{-4} \Delta S_1 = \frac{2}{3} \rightarrow \Delta S_1 = \frac{2}{3} \cdot \left(\frac{-1}{5,72 \times 10^{-6}} \right) = -116550 \text{ m}$

$\tau = 2/3$ ou p

2) $\tau_\lambda = -0,03 \cdot 2,2 \times 10^{-4} \Delta S_2 = \frac{2}{3}$

$\Delta S_2 = \frac{2}{3} \cdot \left(\frac{-1}{6,6 \times 10^{-6}} \right) = -101010 \text{ m} = -101 \text{ Km}$

$\therefore \tau = 2/3$ vale para as profundidades de 116 Km e 101 Km

